

On m-convexity of $C_b(X,A)$ and $C_p(X,A)$

Let X be a completely regular Hausdorff space and A be a topological algebra. We denote by $C(X,A)$ the algebra of all continuous functions on X valued in a complex commutative unital m -convex algebra A . Let $C_b(X,A)$ be its subalgebra consisting of all bounded continuous functions and $C_p(X,A)$ is the subalgebra of $C_b(X,A)$ of all bounded continuous f such that the closure of its range in A is compact in A . A locally convex algebra is a topological algebra A which is a locally convex space. In this case its topology can be given by a family $\{|\cdot|_\alpha : \alpha \in \Lambda\}$ of seminorms satisfying the following condition: for every $\alpha \in \Lambda$ there exist β such that $\|xy\|_\alpha \leq \|x\|_\beta \|y\|_\beta$ for all $x, y \in A$. A locally convex algebra is said to be m -convex (multiplicatively convex) if every seminorm is submultiplicative, i.e. the above inequality can be replaced by $\|xy\|_\alpha \leq \|x\|_\alpha \|y\|_\alpha$ for all $\alpha \in \Lambda$ and all $x, y \in A$. We give conditions on the m -convexity of $C_b(X,A)$ and $C_p(X,A)$.